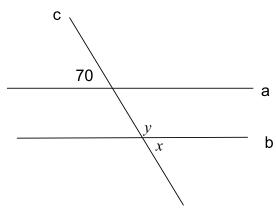
## Solutions to Chapter 34: ANGLES

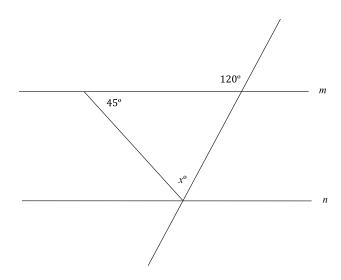


- 1. In the given figure, line a is parallel to line b, and line c intersects both lines. Which of the following statements is true?
- A) The value of y is 70 degrees
- B) The value of x is 70 degrees
- C) The value of x is 110 degrees
- D) The values of x and y cannot be determined from the information given

## Solution Strategy:

Since lines a and b are parallel, and line c is a straight line crossing a and b, then all big angles are equal and all small angles are equal. Since angle x is a small angle, it also equals 70 degrees.

Correct Answer: B

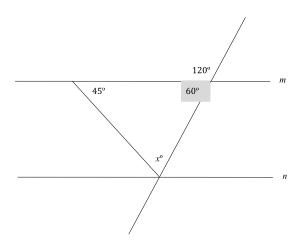


2. In the figure above, if line m is parallel to line n, what is the value of x?

- A) 115°
- B) 75°
- C) 65°
- D) 45

Step 1: Label

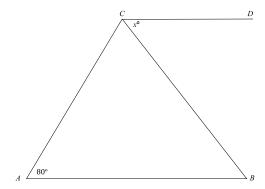
Since we know the measure of a line is  $180^{\circ}$ , this means that the angle directly below and to the left of 120 must be 60. 180 - 120 = 60



Step 2: Carve out the triangle

Recognizing that the figure is a triangle, and a triangle has  $180^{\circ}$ , the third angle of the triangle (x) must be:  $180-45-60=75^{\circ}$ 

Correct Answer: B



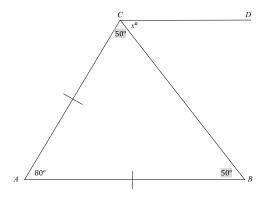
3. In the figure above,  $\overline{AB} \simeq \overline{AC}$  and  $\overline{AB} \parallel \overline{CD}$ . What is the value of x in degrees?

- A) 30
- B) 40
- C) 50
- D) 80

Step 1: Label

Since we are given that  $\overline{AB} \simeq \overline{AC}$  we have an isosceles triangle, which is a triangle with 2 equal sides. Since angles opposite equal sides must also be equal, angles ACB and ABC are equal. Since a triangle has  $180^{\circ}$ , we can subtract  $80^{\circ}$  from  $180^{\circ}$  and then divide by 2 to find both angles:

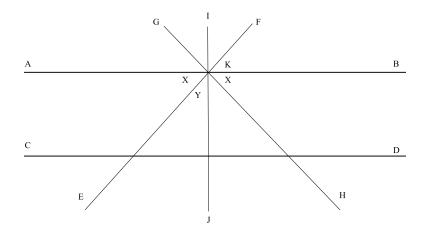
$$180 - 80 = 100 \div 2 = 50^{\circ}$$



Step 2: Since  $\overline{AB} \parallel \overline{CD}$ , understand that angle B and angle x are alternate interior angles since they are inside parallel lines and cut by a transversal.

Therefore the angles will be equal to each other and  $x^{\circ} = 50^{\circ}$ 

Correct Answer: C



4. In the figure above,  $\overline{AB} \parallel \overline{CD}$  and  $\overline{II}$  bisects  $\angle$ EKH. Which of the following is equal to 4y in terms of x?

- A) 360 4x
- B) 180 3x
- C) 360 + 4x
- D) 180 + 2x

Step 1: Since  $\overline{IJ}$  bisects  $\angle EKH$  the angle directly to the right of Y is also equal to Y

Step 2: So now below the line  $\overline{AB}$  we have X, X, Y, Y. We know the sum of these 4 angles is equal to 180° since that is how many degrees are in a line.

$$X + X + Y + Y = 180^{\circ}$$
  
 $2X + 2Y = 180^{\circ}$ 

Step 3: Now we want to take our equation and solve for Y

$$2X + 2Y = 180^{\circ}$$

Divide equation by  $2 \rightarrow X + Y = 90$ 

Subtract *X* to other side  $\rightarrow$  *Y* = 90 - *X* 

Step 4: Now to find 4Y, multiple the entire equation by 4.

$$4(Y = 90 - X) \rightarrow 4Y = 360 - 4X$$

Correct Answer: A

## Or Plugging In might be quicker:

Step 1: Identify a variable(s) to plug in.

Since x shows up the most and is in the answer choices, let's plug in for x. Let's try 40°.

Step 2: Work the steps of the problem.

Step 3: Put a TV around the Target Value.

From above we know that  $X + X + Y + Y = 180^{\circ}$ ,  $2X + 2Y = 180^{\circ}$ 

Plugging in x = 40, gives us:

$$2(40) + 2y = 180$$

$$80 + 2y = 180$$

$$2y = 100$$

$$y = 50$$

Therefore, 4y = 200

## Step 4: Check each answer choice to find your Target Value.

When we plug in x = 40, we need a TV of 200.

A) 
$$360 - 4x$$
  $360 - 4(40) = 200$ 

B) 
$$180 - 3x$$
  $180 - 3(40) = 60$ 

C) 
$$360 + 4x$$

$$360 + 4(40) = 520$$

D) 
$$180 + 2x$$

$$180 + 2(40) = 260$$

Correct Answer: A